# Dynamic approach of spatial segregation: a framework with mobile phone data 

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# Introduction 

Residential segregation drivers

## Residential segregation drivers: housing

- Income gradient from housing prices (Alonso, 1964)
- High opportunity cost of transportation: wealthiest live in city center, poorest in suburbs
- High valuation of housing space: wealthiest live in suburbs, poorest in city center
- Social housing aims to ensure social mixing
- Social housing clusters poor population in specific areas (Verdugo and Toma, 2018)
- Dynamic effect: school segregation creates persistence - People can coexist without interaction (Chamboredon and Lemaire, 1970)


## Residential segregation drivers: preferences and mobility

- Heterogeneity in preferences have spatial effects
- Schelling (1969): clustering based on preference for neighborhood
- Tiebout (1956): spatial sorting based on public goods preferences
- Mobility plays a key role to understand segregation
- Long run: high quality public good bring people in neighborhood, affecting housing price (Black, 1999; Fack and Grenet, 2010)
- Within-week mobility brings together people from different neighborhood
- Infraday dynamic can be strong:
- Davis et al. (2017): outside segregation (restaurants) $50 \%$ lower than residential segregatio
- Athey et al. (2019): similar scale for public space as parks


## Residential segregation: limitations of tax data

- Good picture of residential segregation with tax \& census data
- But fixed picture
- People spend time out of their living neighborhood:
- Experienced segregation vs residential segregation

(a) Low-income population (first decile)

(b) High-income population (last decile)


## Residential segregation: limitations of tax data

- Dissimilarity index (Duncan \& Duncan, 1955)

$$
I D=\frac{1}{2} \sum_{j=1}^{J}\left|\frac{w_{j}}{W_{T}}-\frac{n_{j}-w_{j}}{N_{T}-W_{T}}\right|
$$

- Administrative data $\Rightarrow$ residential segregation:
- Static vision of segregation
- Separation of income groups within residential space
- No information on visited places
- Mobility continuously reshapes income spatial distribution
- Need high-frequency geolocated data...
- ... combined with traditional data to characterize individuals


# Research question 

## Research question

- Main questions:
- How do mobility affect urban segregation ?
- Do high-frequency data help us in identifying patterns in segregation that cannot be understood with administrative data?
- Contribution:
- Combining phone and traditional data
- Proposition of a methodology to ensure combination robustness
- Fine spatial and temporal granularity to understand segregation
- Next step is to interpret patterns with respect to city characteristics


## Methodology adopted

- We analyze infraday dynamic:
- 48 points: 24 for weekdays, 24 for weekend
- Requires time depending segregation indexes
- Dissimilarity index series for each city
- Paris, Lyon and Marseilles
- Agglomeration level: city centers and suburbs
- More than 13 millions people in tax data
- More cities soon


#### Abstract

Data


## Principle

- Caracterize phone users from living environment
- Probability of belonging to first/last decile from observed income distribution in tax data


Phone data

## Phone data

- Orange data September 2007
- 18.5 millions SIM cards ( $\approx 1 / 3$ French population)
- Text messages and call: 3 billions events
- Geocoding at antenna level (exact $(x, y)$ unknown)
- Transformation into $500 \times 500$ meters cell level presence


## Methodology here

- We do not use interaction dimension
- Plan for future research on social segregation
- Big data volume is a challenge


## Phone data

- 2007 is old:
- People were not using their phone as much as now
- Temporal sparsity at individual level (in average 4 points a day by user)

|  | mean | s.d. | $\min$ | P 10 | P 25 | median | P 75 | P 90 | $\max$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Average number of daily events per <br> user | 4.3 | 3.6 | 1 | 1.4 | 2 | 3.1 | 5.4 | 8.7 | 123 |
| Number of distincts days users ap- <br> pear | 20 | 9.2 | 1 | 5 | 13 | 23 | 28 | 30 | 30 |
| Average number of events between <br> 7PM and 9AM per user | 2.4 | 1.7 | 0 | 1 | 1.3 | 1.9 | 2.9 | 4.4 | 87 |
| Number of distincts days users ap- <br> pear between 7PM and 9AM | 15.2 | 9.4 | 0 | 2 | 7 | 15 | 24 | 28 | 30 |
| Number of observations: <br> Number of unique phone users: |  |  | $3,024,884,663$ |  |  |  |  |  |  |
| $18,541,440$ |  |  |  |  |  |  |  |  |  |

Table 1: Orange 2007 CDR : summary statistics of September data [replace and update the one in the paper]

Tax data

## Tax data

- 2011 geocoded tax data at $(x, y)$ level
- Income by consumption unit
- Income based segregation
- Distribution of income extremes (first and last deciles)
- Relative definition of income: is individual wealthier/poorer than a city reference level ?
- Bimodal approach
- First decile vs others
- Last decile vs others


## Tax data

- Sub-population (first/last decile) frequency in cell
- Spatial aggregation at cell level $i$

$$
\begin{aligned}
& p_{i}^{D 1}=\mathbb{P}\left(y_{x}<\mu^{D 1}\right)=\mathbb{E}\left(\mathbf{1}_{\left\{y_{x}<\mu^{D 1}\right\}}\right)=\frac{1}{n_{i}} \sum_{x=1}^{n_{i}} \mathbf{1}_{\left\{y_{x}<\mu^{D 1}\right\}} \\
& p_{i}^{D 9}=\mathbb{P}\left(y_{x}>\mu^{D 9}\right)=\mathbb{E}\left(\mathbf{1}_{\left\{y_{x}>\mu^{D 9}\right\}}\right)=\frac{1}{n_{i}} \sum_{x=1}^{n_{i}} \mathbf{1}_{\left\{y_{x}>\mu^{D 9}\right\}}
\end{aligned}
$$

- If $p_{i}>0.1$, over-representation of subpopulation in cell
- That frequency is used to simulate phone user status given their simulated residence


## Tax data

- Intuitions regarding city segregation from tax data
- e.g. Paris: more segregation at the top


Figure 2: Dissimilarity index for main French cities

## Methodology to build segregation index

## Workflow

- Phone user status is simulated from his/her phone track (only personal information) and neighborhood level tax aggregates
- 3 steps to estimate segregation dynamics:

1. Home estimation

- Estimate probabilities that individual lives in some neighborhood given nighttime ( $19 \mathrm{pm}-9 \mathrm{am}$ ) phone track

2. Home cell and income simulations

- Home simulation knowing cell level probability sequences
- Income simulation given first/last decile frequence appearance in tax data $\left(p_{i}\right)$
- Test other designs to check robustness of income simulation

3. Compute segregation indexes
$\checkmark$ They depend on observation time $t$ (dynamic approach)

Details for step 1 and 2 here

## Segregation index

- Two typical days: weekdays, weekend
- Individual probabilities at cell level on a given time window:

$$
\mathbb{P}_{x}\left(c_{i t}\right)
$$

- Probabilize dissimilarity index (Duncan \& Duncan, 1955):
- Remainder, standard index:

$$
I D=\frac{1}{2} \sum_{c \in \mathcal{C}}\left|\frac{w_{c}}{W_{T}}-\frac{n_{c}-w_{c}}{N_{T}-W_{T}}\right|
$$

Results

Segregation dynamics

## Segregation dynamics: low-income

- City-level segregation evolution across time
- People not observed at a given hour of the night (19-9) are assumed to be at home
- This removes downward bias in index with respect to tax data
- Dynamic robust to other income simulation methods


Figure 3: Low-income segregation dynamics

## Segregation dynamics: high-income



Figure 4: High-income segregation dynamics

## Segregation dynamics: comparing cities and income groups

- Significant difference between nighttime and daytime segregation levels
- Segregation starts to decrease around 6-7am and goes up after 4-5pm
- No significant difference between weekend and weekdays $\Rightarrow$ separate saturday and sunday?
- Differences in level observed in tax data also present in phone data
- e.g. Paris: segregation higher at the top
- Mobile phone inform us on dynamics:
- Decrease stronger in Marseilles and Lyon than in Paris
- Further research: can we identify some inclusive/exclusive cities ?


## Evolution of city structure across time

e.g. Low-income concentration at two different hours (Full sequence here)

Hour 11


Hour 23

0.5 to 1.0
1.0 to 1.5
1.061 .5
1.5620
2.05025
2.0602 .5
2.5030
2.5 to 3.0
3.060 .5
3
3.0 to 3.5
3.5 to 4.0

## Spatial clustering [really preliminary]

- Clustering to identify spaces that share common population composition characteristics
- Will be related to places characteristics (infrastructures...)
- e.g.: share of population belonging to low-income group



## Spatial clustering [really preliminary]

| Cluster | Night | Day |
| :---: | :---: | :---: |
| 1 | Large over-representation | Decrease |
| 2 | Large over-representation | More stable |
| 3 | Under-representation | Small increase |
| 4 | Large under-representation | Increase |
| 5 | Stable at $10 \%$ | Stable at $10 \%$ |



# Conclusion 

## Conclusion

- Bringing together phone and tax data requires methodological foundations
- Segregation at its acme during nighttime/hometime
- Need interpretation of segregation spatio-temporal dynamics with respect to city amenities
- Results consistent with Davis et al (2017) and Athey et al (2019)


## Appendix

# Probabilization 

## Phone users' presence probabilization



- Mobile phone litterature does not dissociate:
- Coverage area: observations at antenna level into presence area
- Statistical unit: economic information level
- Coverage area: Voronoi tesselation
- Each point in space is associated with closest antenna
- However, must not be analysis statistical unit
- Partition depends too much on antennas local density


## Phone users' presence probabilization

- Cell level probabilization to abstract from voronoi
- Knowing call has been observed from antenna $v_{j}$, probability it happened into cell $c_{i}$ ? (Bayes rule)
- $500 \times 500 \mathrm{~m}$ cell level
- Phone data: probabilize both presence and home
- Tax data: local aggregates at cell level






Methodology: more details

## 1. Home estimation

- Nighttime phone track (19h-9h) used to estimate individual residence probability for all cells
- Bayesian approach to account for the fact that all metropolitan space is not residential
- In a coverage area, prior in most densily populated cells
- Prior from population density computed from tax data
- Prior distribution is a reweighting for cell level home

$$
\mathbb{P}_{x}\left(c_{i}^{\text {home }} \mid v_{j}\right) \propto \underbrace{\mathbb{P}\left(c_{i}^{\text {home }}\right)}_{\begin{array}{c}
\text { prior from } \\
\text { population density }
\end{array}} \underbrace{\mathbb{P}_{x}\left(v_{j} \mid c_{i}\right)}_{\begin{array}{c}
\text { areas ratio: } \\
\frac{s(v \cap c)}{s(c)}
\end{array}}
$$

- Sequence from home probabilities: $\nu_{x}^{\text {home }}\left(c_{i}\right)$
- Used to simulate $x$ income


## 2. Home and income simulations

4 methods of home simulation to check robustness of segregation indexes

| Methodology | Choice of $x$ 's home |
| :--- | :--- |
| Main method | Draw home from all residence probabilities $\nu_{x}^{\text {home }}$ |
| One stage | Cell where probability is maximum: $c_{i}=$ |
| simulation | $\arg \max _{c_{i}} \nu_{x}^{\text {home }}\left(c_{i}\right)$ |
| cell_max_proba | $x$ assigned where probability of being member of <br> group $g$ is maximized <br> cell_min_proba |
|  | $x$ assigned where probability of being member of <br> group $g$ is minimized |

Last two methods: evaluate effect on segregation indexes to over- or under-estimate the share of sub-group $g$ on population

## 3. Segregation indexes: cell level presence

- Probability that an event measured in antenna $v_{j}$ at time $t$ occurred in cell $c_{i}$ is

$$
p_{i}^{j}:=\mathbb{P}\left(c_{i} \mid v_{j}\right)=\frac{\mathbb{P}\left(c_{i} \cap v_{j}\right)}{\mathbb{P}\left(v_{j}\right)}=\frac{\mathcal{S}\left(c_{i} \cap v_{j}\right)}{\mathcal{S}\left(v_{j}\right)}
$$

- We denote $c_{i t}$ the probability of being present at time $t$ in cell $c_{i}$. This is a recollection of conditional probabilities

$$
\begin{equation*}
\forall c_{i t} \in \mathcal{C}, \quad \mathbb{P}_{x}\left(c_{i t}\right)=\sum_{v_{j t} \in \mathcal{V}} \mathbb{P}\left(c_{i t} \mid v_{j t}\right) \mathbb{P}_{x}\left(v_{j t}\right) \tag{1}
\end{equation*}
$$

with $\mathcal{V}$ voronoi/antennas and $\mathcal{C} 500 \mathrm{~m}$ cells.

